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# The Elasticity of Substitution in Demand for Non-Tradable Goods in Latin America: The Case of Argentina 

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#### Abstract

The objective of this paper is to estimate the elasticity of substitution in the demand for non-tradable goods relative to tradable goods in Argentina. This parameter plays a crucial role in the analysis of the macroeconomic equilibrium of a small open economy (Mendoza, Galindo and Izquierdo, 2003). Using two data sets, estimates of approximately 0.40 and 0.48 , respectively, are found for this elasticity.


## 1. Methodology and Data

Consider a small open economy with tradable goods, $T$, and non-tradable goods, $N$. The consumer's preferences for these two goods are described by the utility function

$$
\begin{aligned}
U\left(C_{t}^{T}, C_{t}^{N}\right) & =\left(\omega\left(C_{t}^{T}\right)^{-\eta}+(1-\omega)\left(e^{u_{t}}\right)\left(C_{t}^{N}\right)^{-\eta+\theta}\right)^{-\frac{1}{\eta}} \quad \text { for } \eta \neq \theta \\
& =\left(\omega\left(C_{t}^{T}\right)^{-\eta}+(1-\omega)\left(e^{u_{t}}\right) \ln \left(C_{t}^{N}\right)\right)^{-\frac{1}{\eta}} \quad \text { for } \eta=\theta
\end{aligned}
$$

where $C_{t}^{T}, C_{t}^{N}$ denote the consumption of tradable and non-tradable goods, $\eta>1, \omega>0$, and $u_{t}$ are normally distributed preference shocks. If the parameter $\theta$ differs from zero, preferences are not homothetic and there will be income effects on the relative demand for tradable and non-tradable goods. A positive $\theta$ implies that $N$ goods are superior goods. ${ }^{1}$

Households maximize $E \sum \beta^{t} U\left(C_{t}^{T}\left(s^{t}\right), C_{t}^{N}\left(s^{t}\right)\right)$ subject to the budget constraint

$$
A_{0}+\sum_{t=0}^{\infty} p\left(s^{t}\right)\left(Y_{t}^{d}\left(s^{t}\right)-p_{t}^{N}\left(s^{t}\right) C_{t}^{N}\left(s^{t}\right)-C_{t}^{T}\left(s^{t}\right)-\left(K_{t+1}\left(s^{t}\right)-(1-\delta) K_{t}\left(s^{t}\right)\right)\right) \geq 0
$$

where $s^{t}$ denotes the history of the economy up to period $t, A_{0}$ is the initial financial wealth, $p\left(s^{t}\right)$ is the price of a unit of good $T$ consumption in state $s^{t}$ in terms of units of good $T$ at time $0, Y_{t}^{d}$ is the household's disposable income measured in tradable goods, $p_{t}^{N}$ is the relative price of non-tradable goods, and $K_{t+1}-(1-\delta) K_{t}$ denotes the accumulation of capital and $K_{0}$ is given. If asset markets are incomplete or there are

[^0]participation constraints, $p\left(s^{t}\right)$ are interpreted as the marginal utility of wealth in state $s^{t}$ for some agents and the consumer would face additional constraints.

The first-order conditions for this problem imply the equilibrium relation

$$
\begin{equation*}
\ln \left(\frac{C_{t}^{N}}{C_{t}^{T}}\right)=\frac{1}{1+\eta} \ln \frac{1-\omega}{\omega}-\frac{1}{1+\eta} \ln p_{t}^{N}+\frac{\theta}{1+\eta} C_{t}^{N}+\varepsilon_{t} \tag{1}
\end{equation*}
$$

where $\varepsilon_{t}$ can be interpreted as a composition of the preference shocks $u_{t}$ and measurement error. The parameter of interest, the elasticity of substitution in the demand for nontradable goods relative to tradable goods is $v \equiv \frac{1}{1+\eta}$.

The estimation of the elasticity of substitution in the demand for non-tradable goods relative to tradable goods in Argentina was performed with data obtained from official sources. Two data sets were obtained for the period 1993-2001. The first one contains data on the consumption of tradable and non-tradable goods constructed from the national income and product accounts following the flow of goods approach suggested in the terms of reference for this project (Mendoza, Galindo and Izquierdo, 2003). That is, consumption in sector $i$ is calculated from the equation $C_{i}=Y_{i}-\sum_{j} I C_{i j}-\left(X_{i}-M_{i}\right)-I_{i}$, where $C_{i}, Y_{i}, X_{i}, M_{i}, I_{i}$ denote consumption, gross production, exports, imports and investment in sector $i$ and $I C_{i j}$ denotes the intermediate consumption of good $i$ in sector $j .{ }^{2}$ The corresponding prices are the implicit prices in the national income accounts. The second data set employed in this study uses data on the consumption of non-durable goods (tradable goods) and services (nontradable goods) and price indices for these categories of goods computed from the consumer price index data set.

[^1]
## 2. Estimation Results

The first step in the estimation procedure is to transform the data by computing the relevant variables in logs. Figure 1 shows the $\log$ of real tradable and non-tradable consumption from the first quarter of 1993 to the third quarter of 2001. As the figure indicates, the presence of seasonality is clear in both series.

Figure 1.
Consumption of Tradable and Non-Tradable Goods


The next figure plots the implicit prices of non-tradable and tradable goods. Seasonality is less noticeable in this plot, at least for tradable prices.

Figure 2.
Non-Tradable and Tradable Prices


Finally, Figure 3 shows the ratio of non-tradable to tradable consumption and prices in logs. One feature of this final graph is the absence of seasonality in both ratios.

Figure 3.
Non-Tradable and Tradable Consumption and Prices


The time trend in the ratio of the ratio of the consumption of non-tradable to non-tradable goods motivates the flexible functional form for preferences that allows for the nonhomothetic case.

Since the dataset comprises variables varying with time, the next task is to check the order of integration of each variable individually. In order to do this, the standard augmented Dickey-Fuller test (see Dickey and Fuller, 1979) was applied to each variable. Table 1 summarizes the results.

Table 1. Unit Root Tests

| Variable ADF t-Statistic p-Value | Lags |  |  |
| :--- | :--- | :--- | :--- |
| $\ln \left(C_{t}^{N} / C_{t}^{T}\right)$ | -0.057 | 0.9454 | 4 |
| $\ln \left(p_{t}^{N}\right)$ | -1.926 | 0.3167 | 0 |
| $\ln \left(C_{t}^{N}\right)$ | -1.195 | 0.6631 | 4 |
| $\ln \left(C_{t}^{T}\right)$ | -2.252 | 0.1932 | 4 |

Notes: The number of lags in the test was selected using the Schwartz Information Criterion. The probability of rejection was computed using MacKinnon (1996) one-sided p-values.

Augmented Dickey-Fuller tests on the variables show the presence of a unit root in each of the series. Therefore, before going to the estimation step it is necessary to check for cointegration among the variables of the model. Table 2 shows Johansen's cointegration test (see Johansen, 1991) among the ratio between consumption of nontradable and tradable goods, the ratio between the prices of the non-tradable and tradable goods and the consumption of non-tradable goods in logarithms and expressed in real terms.

Table 2. Johansen Cointegration Test

| Null Hypothesis | Eigenvalue | Trace Statistic | 5\% Critical Value | 1\% Critical Value |
| :--- | :---: | :---: | :---: | :---: |
| None | 0.675 | 47.185 | 29.68 | 35.65 |
| At most one | 0.2762 | 15.716 | 15.41 | 20.04 |
| At most two | 0.2119 | 6.666 | 3.76 | 6.65 |
| Null Hypothesis | Eigenvalue | Trace Statistic | $\mathbf{5 \%}$ Critical Value | $\mathbf{1 \%}$ Critical Value |
| None | 0.675 | 31.469 | 20.97 | 25.52 |
| At most one | 0.2762 | 9.05 | 14.07 | 18.63 |
| At most two | 0.2119 | 6.666 | 3.76 | 6.65 |

Note: The number of lags in the test was selected using the Schwartz Information Criterion.
As indicated in the table above, both test statistics (the trace and maximum eigenvalue) indicate the presence of cointegration at the 1 percent level and the maximum eigenvalue statistic also indicates cointegration at the 5 percent level. Therefore, there is evidence of cointegration among the variables as predicted by the theoretical model.

The next step is to estimate the model. In order to do this a vector error correction model is estimated for the three variables. The specification of the error correction model corresponds to the six lags selected in the cointegration test and includes three dummy variables to account for the seasonal cycles. The estimated error correction equation is presented below. ${ }^{3}$

$$
\begin{gathered}
\ln \left(\frac{C_{t}^{N}}{C_{t}^{T}}\right)=14.96-0.4034 \ln p_{t}^{N}+0.5954 \ln C_{t}^{N} \\
(0.20)
\end{gathered}
$$

[^2]All estimated coefficients are statistically significant at the usual significance levels. Equation (2) indicates that the long-run elasticity of substitution between tradable and non-tradable goods is about -0.40 , which is closer to the estimate of 0.44 obtained by Stockman and Tesar (1995) than the estimate of 0.74 obtained by Mendoza (1995). The coefficient on $C_{t}^{N}$ is tightly estimated and indicates strong income effects. The point estimates of the preference parameters are about $\eta=\theta=1.47$.

In order to have an alternative estimation of the elasticity of substitution the procedure described above is repeated, but this time the consumption of non-durable goods is used as a proxy for the consumption of tradable goods, and the consumption of services as a proxy for the consumption of non-tradable goods. The implicit prices of non-durable goods and services are used to construct the ratio between the prices of nontradable and tradable goods. The Appendix shows unit root tests for the individual variables, the Johansen's cointegration test and the vector error correction estimation. In this case, the cointegration results are somewhat weaker. Only the maximum eigenvalue test indicates cointegration at the 1 percent level. Consistent with this result, using this specification an estimation of the elasticity of substitution of approximately -0.48 is obtained, statistically significant at the 10 percent level.

## 3. Final Remarks

Using data for the 1980s and 1990s, this paper has estimated the elasticity of substitution between tradable and non-tradable goods for Argentina to be between approximately 0.40 and 0.48 .

In spite of the small number of observations and the possible measurement error in the data, the error correction model detected a long-run equilibrium relation between the ratio of consumption of tradable and non-tradable goods, their relative prices and the level of consumption in non-tradable goods. Moreover, the estimated model is consistent with the theory and with Stockman and Tesar's (1995) estimate of the parameter of interest for a sample of developed countries.

However, it is worth mentioning that a small sample of time series variables was used, and this had implications for the estimation. On one hand, the short time series did not permit the use of exogenous variables in the vector error correction specification
because of the limited degrees of freedom. On the other hand, the estimated model is not very robust, in the sense that the selected estimation does not present very stable estimated coefficients.

## 5. References

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## Appendix

Table 1.A. Vector Error Correction Model Estimation Results

| Cointegration Eq: $\quad z_{t-1}$ |  |  |  |
| :---: | :---: | :---: | :---: |
| $\ln \left(C_{N T t-1} / C_{T_{t-1}}\right)$ | 1 |  |  |
| $\ln \left(P_{N T t-1} / P_{T_{t-1}}\right)$ | $0.4034$ |  |  |
|  | [2.0021] |  |  |
| $\ln \left(C_{N T t-1}\right)$ | -0.5954 |  |  |
|  | (0.0527) |  |  |
|  | [-11.3061] |  |  |
| C | 14.9634 |  |  |
| Error Correction: | $\Delta\left(\ln \left(C_{N T} / C_{T}\right)\right)$ | $\Delta\left(\ln \left(P_{N T} / P_{T}\right)\right)$ | $\Delta\left(\ln C_{N T}\right)$ |
| $z_{t-1}$ |  |  |  |
|  | -0.469200 | -0.481383 | -0.285831 |
|  | (0.49994) | (0.36038) | (0.19651) |
|  | [-0.93851] | [-1.33577] | [-1.45456] |
| $\Delta\left(\ln \left(C_{N T} / C_{T}\right)_{t-1}\right)$ |  |  |  |
|  | 0.612304 | 0.519411 | -0.337430 |
|  | (0.63025) | (0.45431) | (0.24773) |
|  | [0.97153] | [1.14330] | [-1.36211] |
| $\Delta\left(\ln \left(C_{N T} / C_{T}\right)_{t-2}\right)$ |  |  |  |
|  | -0.588071 | -0.071664 | 0.232468 |
|  | (0.61440) | (0.44288) | (0.24150) |
|  | [-0.95714] | [-0.16181] | [0.96261] |
| $\Delta\left(\ln \left(C_{N T} / C_{T}\right)_{t-3}\right)$ |  |  |  |
|  | -0.598401 | 0.599062 | -0.330187 |
|  | (0.68513) | (0.49387) | (0.26930) |
|  | [-0.87341] | [1.21299] | [-1.22610] |
| $\Delta\left(\ln \left(C_{N T} / C_{T}\right)_{t-4}\right)$ |  |  |  |
|  | -0.077077 | 0.401242 | 0.524183 |
|  | (0.77212) | (0.55657) | (0.30349) |
|  | [-0.09983] | [0.72092] | [1.72720] |
| $\Delta\left(\ln \left(C_{N T} / C_{T}\right)_{t-5}\right)$ | $0.540688$ | 0.451324 | $-0.114233$ |
|  |  |  |  |
|  | (0.64847) | (0.46744) | (0.25489) |
|  | [0.83379] | [0.96552] | [-0.44817] |

Table 1.A., continued

| Error Correction: | $\Delta\left(\ln \left(C_{N T} / C_{T}\right)\right)$ | $\Delta\left(\ln \left(P_{N T} / P_{T}\right)\right)$ | $\Delta\left(\ln C_{N T}\right)$ |
| :---: | :---: | :---: | :---: |
| $\Delta\left(\ln \left(C_{N T} / C_{T}\right)_{t-6}\right)$ |  |  |  |
|  | 0.220120 | 0.277890 | 0.455729 |
|  | (0.63516) | (0.45785) | (0.24965) |
|  | [0.34656] | [0.6695] | [1.82544] |
| $\Delta\left(\ln \left(P_{N T} / P_{T}\right)_{t-1}\right)$ |  |  |  |
|  | -0.832011 | 0.028274 | -0.689081 |
|  | (0.62962) | (0.45385) | (0.24748) |
|  | [-1.32146] | [0.06230] | [-2.78443] |
| $\Delta\left(\ln \left(P_{N T} / P_{T}\right)_{t-2}\right)$ |  |  |  |
|  | -0.111923 | -0.421696 | -0.004859 |
|  | (0.78471) | (0.56565) | (0.30844) |
|  | [-0.14263] | [-0.74551] | [-0.01575] |
| $\Delta\left(\ln \left(P_{N T} / P_{T}\right)_{t-3}\right)$ |  |  |  |
|  | -0.499180 | -0.336285 | -0.307264 |
|  | (0.83229) | (0.59995) | (0.32714) |
|  | [-0.59977] | [-0.56053] | [-0.93925] |
| $\Delta\left(\ln \left(P_{N T} / P_{T}\right)_{t-4}\right)$ |  |  |  |
|  | -0.328235 | -0.513406 | 0.246264 |
|  | (0.79898) | (0.57593) | (0.31405) |
|  | [-0.41082] | [-0.89143] | [0.78417] |
| $\Delta\left(\ln \left(P_{N T} / P_{T}\right)_{t-5}\right)$ |  |  |  |
|  | -0.187846 | -0.172702 | -0.332842 |
|  | (0.72347) | (0.52150) | (0.28437) |
|  | [-0.25965] | [-0.33116] | [-1.17047] |
| $\Delta\left(\ln \left(P_{N T} / P_{T}\right)_{t-6}\right)$ |  |  |  |
|  | -0.306048 | -0.109493 | -0.098211 |
|  | (0.65486) | (0.47205) | (0.25740) |
|  | [-0.46735] | [-0.23195] | [-0.38155] |
| $\Delta\left(\ln C_{N T t-1}\right)$ |  |  |  |
|  | -2.457124 | -0.735731 | 0.016370 |
|  | (1.28354) | (0.92522) | (0.50451) |
|  | [-1.91434] | [-0.79519] | [0.03245] |
| $\Delta\left(\ln C_{N T t-2}\right)$ |  |  |  |
|  | -0.544635 | 0.463027 | -1.014808 |
|  | (1.06280) | (0.76610) | (0.41774) |
|  | [-0.51245] | [0.60429] | [-2.42927] |
| $\Delta\left(\ln C_{N T t-3}\right)$ |  |  |  |
|  | -0.419562 | -0.682683 | 0.619423 |
|  | (1.04856) | (0.75584) | (0.41215) |
|  | [-0.40013] | [-0.90321] | [1.50292] |

Table 1.A., continued

| Error Correction: | $\Delta\left(\ln \left(C_{N T} / C_{T}\right)\right)$ | $\Delta\left(\ln \left(P_{N T} / P_{T}\right)\right)$ | $\Delta\left(\ln C_{N T}\right)$ |
| :---: | :---: | :---: | :---: |
| $\Delta\left(\ln C_{N T_{t-4}}\right)$ |  |  |  |
|  | -0.258799 | 0.041919 | -0.513012 |
|  | (1.16045) | (0.83650) | (0.45613) |
|  | [-0.22302] | [0.05011] | [-1.12472] |
|  |  |  |  |
|  | -0.624372 | 0.216330 | 0.590741 |
|  | (1.11351) | (0.80266) | (0.43768) |
|  | [-0.56072] | [0.26952] | [1.34972] |
| $\Delta\left(\ln C_{N T_{t-6}}\right)$ |  |  |  |
|  | 0.842801 | -0.106746 | -0.407851 |
|  | (0.89261) | (0.64342) | (0.35085) |
|  | [0.94420] | [-0.16590] | [-1.16247] |
| C | -0.045699 | -0.103508 | 0.200619 |
|  | (0.15699) | (0.11316) | (0.06171) |
|  | [-0.29110] | [-0.91469] | [3.25125] |
| DUMMY 1st Quarter | 0.135672 | 0.141469 | -0.389241 |
|  | (0.30588) | (0.22049) | (0.12023) |
|  | [0.44354] | [0.64161] | [-3.23746] |
| DUMMY 2nd Quarter | -0.130081 | 0.023923 | 0.08674 |
|  | (0.12335) | (0.08891) | (0.04848) |
|  | [-1.05460] | [0.26906] | [0.17891] |
| DUMMY 3rd Quarter | 0.29444 | 0.180465 | -0.396348 |
|  | (0.36101) | (0.26023) | (0.14190) |
|  | [0.81561] | [0.69348] | [-2.79318] |
| R-squared | 0.867471 | 0.747891 | 0.987182 |
| Sum sq. Resids. | 0.005254 | 0.02730 | 0.000812 |
| Log likelihood | 80.40316 | 89.56866 | 106.5494 |

Notes: Standard error in () and t-statistics in [ ].
Tables 2.A, 3.A and 4.A show unit root tests, cointegration test and estimation results for the alternative representation of non-tradable and tradable goods. That is, as mentioned above in the main text, consumption of non-tradable goods is approximated by the consumption of services, while consumption of tradable goods is approximated by the consumption of non-durable goods. The ratio of prices of services to non-durable goods thus approximates the ratio of non-tradable and tradable prices.

Table 2.A. Unit Root Tests

| Variable | ADF t-Statistic | p-Value | Lags |
| :--- | :---: | :---: | :---: |
| $\ln \left(C_{t}^{N} / C_{t}^{T}\right)$ | -0.265 | 0.9202 | 0 |
| $\ln \left(p_{t}^{N}\right)$ | -1.121 | 0.6964 | 0 |
| $\ln \left(C_{t}^{N}\right)$ | -1.599 | 0.4706 | 5 |
| $\ln \left(C_{t}^{T}\right)$ | -0.089 | 0.9417 | 6 |

Notes: The number of lags in the test was selected using the Schwartz Information Criterion. The probability of rejection was computed using MacKinnon (1996) one sided p-values.

Table 3.A. Johansen's Cointegration Test

| Null Hypothesis | Eigenvalue | Trace Statistic | $\mathbf{5 \%}$ Critical Value | $\mathbf{1 \%}$ Critical Value |
| :--- | :---: | :---: | :---: | :---: |
| None | 0.5915 | 44.372 | 24.31 | 29.75 |
| At most one | 0.3265 | 18.406 | 12.53 | 16.31 |
| At most two | 0.2129 | 6.943 | 3.84 | 6.51 |
| Null Hypothesis | Eigenvalue | Trace Statistic | $\mathbf{5 \%}$ Critical Value | 1\% Critical Value |
| None | 0.5915 | 25.966 | 17.89 | 22.99 |
| At most one | 0.3265 | 11.464 | 11.44 | 15.69 |
| At most two | 0.2129 | 6.943 | 3.84 | 6.51 |

[^3]Table 4.A. Vector Error Correction Model Estimation Results

| Cointegration Eq | $z_{t-1}$ |  |  |
| :---: | :---: | :---: | :---: |
| $\begin{aligned} & \ln \left(C_{N T_{t-1}} / C_{T_{t-1}}\right) \\ & \ln \left(P_{N T_{t-1}} / P_{T_{t-1}}\right) \end{aligned}$ | 1 |  |  |
|  | 0.4987 |  |  |
|  | (0.3656 |  |  |
|  | [1.3639] |  |  |
| $\ln \left(C_{N T t-1}\right)$ | -0.07235 |  |  |
|  | (0.0054) |  |  |
|  | [-13.4077] |  |  |
| Error Correction: | $\Delta\left(\ln \left(C_{N T} / C_{T}\right)\right)$ | $\Delta\left(\ln \left(P_{N T} / P_{T}\right)\right)$ | $\Delta\left(\ln C_{N T}\right)$ |
| $z_{t-1}$ |  |  |  |
|  | -0.131676 | -0.122110 | -0.250651 |
|  | (0.14334) | (0.09749) | (0.07448) |
|  | [-0.91863] | [-1.25257] | [-3.36554] |
| $\Delta\left(\ln \left(C_{N T} / C_{T}\right)_{t-1}\right)$ |  |  |  |
|  | -0.083987 | 0.282037 | -0.217394 |
|  | (0.36609) | (0.24898) | (0.19021) |
|  | [-0.22942] | [1.13276] | [-1.14291] |
| $\Delta\left(\ln \left(C_{N T} / C_{T}\right)_{t-2}\right)$ |  |  |  |
|  | -0.475877 | -0.084897 | 0.473100 |
|  | (0.37538) | (0.25530) | (0.19504) |
|  | [-1.26773] | [-0.33254] | [2.42569] |
| $\Delta\left(\ln \left(C_{N T} / C_{T}\right)_{t-3}\right)$ |  |  |  |
|  | 0.060091 | -0.034825 | -0.488374 |
|  | (0.34514) | (0.23474) | (0.17933) |
|  | [0.17410] | [-0.14836] | [-2.72336] |
| $\Delta\left(\ln \left(C_{N T} / C_{T}\right)_{t-4}\right)$ |  |  |  |
|  | -0.035277 | -0.303725 | -0.133463 |
|  | (0.38780) | (0.26375) | (0.20149) |
|  | [-0.09097] | [-0.15156] | [-0.66237] |
| $\Delta\left(\ln \left(C_{N T} / C_{T}\right)_{t-5}\right)$ |  |  |  |
|  | 0.374066 | -0.137591 | -0.194811 |
|  | (0.34862) | (0.23710) | (0.18114) |
|  | [1.07299] | [-0.58030] | [-1.07550] |
| $\Delta\left(\ln \left(C_{N T} / C_{T}\right)_{t-6}\right)$ |  |  |  |
|  | 0.492397 | 0.047495 | -0.349563 |
|  | (0.42623) | (0.28989) | (0.22146) |
|  | [1.15522] | [0.16384] | [-1.57843] |

Table 4.A., continued

| Error Correction: | $\Delta\left(\ln \left(C_{N T} / C_{T}\right)\right)$ | $\Delta\left(\ln \left(P_{N T} / P_{T}\right)\right)$ | $\Delta\left(\ln C_{N T}\right)$ |
| :---: | :---: | :---: | :---: |
| $\Delta\left(\ln \left(P_{N T} / P_{T}\right)_{t-1}\right)$ |  |  |  |
|  | 0.442236 | -0.301454 | -0.253014 |
|  | (0.51887) | (0.35289) | (0.26959) |
|  | [0.85231] | [-0.85424] | [-0.93851] |
| $\Delta\left(\ln \left(P_{N T} / P_{T}\right)_{t-2}\right) \quad$ l |  |  |  |
|  | 0.800562 | -0.054979 | -0.022033 |
|  | (0.54764) | (0.37246) | (0.28454) |
|  | [1.46183] | [-0.14761] | [-0.07743] |
| $\Delta\left(\ln \left(P_{N T} / P_{T}\right)_{t-3}\right) \quad$ 退 |  |  |  |
|  | 0.615366 | 0.269530 | 0.638819 |
|  | (0.49343) | (0.33559) | (0.25637) |
|  | [1.24712] | [0.80315] | [2.49175] |
| $\Delta\left(\ln \left(P_{N T} / P_{T}\right)_{t-4}\right) \quad$ l |  |  |  |
|  | 0.009219 | 0.689309 | 0.285863 |
|  | (0.52732) | (0.35864) | (0.27398) |
|  | [0.01748] | [1.92201] | [1.04336] |
| $\Delta\left(\ln \left(P_{N T} / P_{T}\right)_{t-5}\right) \quad$ [1.0436] |  |  |  |
|  | -0.060739 | 0.367554 | 0.589934 |
|  | (0.58115) | (0.39525) | (0.30195) |
|  | [-0.10452] | [0.92993] | [1.95375] |
| $\Delta\left(\ln \left(P_{N T} / P_{T}\right)_{t-6}\right)$ |  |  |  |
|  | -0.393692 | 0.304252 | 0.627845 |
|  | (0.59057) | (0.40166) | (0.30685) |
|  | [-0.66663] | [0.75749] | [2.04612] |
| $\Delta\left(\ln C_{N T t-1}\right)$ |  |  |  |
|  | -0.34449 | -0.536003 | 0.559361 |
|  | (0.43270) | (0.29429) | (0.22482) |
|  | [-0.79605] | [-1.82136] | [2.48803] |
| $\Delta\left(\ln C_{N T}{ }^{\text {t-2 }}\right.$ ) |  |  |  |
|  | 0.719131 | 0.122816 | -0.602453 |
|  | (0.57510) | (0.39114) | (0.29881) |
|  | [1.25044] | [0.31400] | [-2.01617] |
| $\Delta\left(\ln C_{N T-3}\right) \quad\left[\begin{array}{l}\text { d }\end{array}\right.$ |  |  |  |
|  | -0.320004 | -0.268406 | 0.039074 |
|  | (0.65475) | (0.44531) | (0.34019) |
|  | [-0.48875] | [-0.60275] | [0.11486] |
| $\Delta\left(\ln C_{N T t-4}\right)$ |  |  |  |
|  | 0.700226 | 0.247096 | 0.009235 |
|  | (0.54524) | (0.37083) | (0.28329) |
|  | [1.28425] | [0.66633] | [0.03260] |

Table 4.A., continued

| Error Correction: | $\Delta\left(\ln \left(C_{N T} / C_{T}\right)\right)$ | $\Delta\left(\ln \left(P_{N T} / P_{T}\right)\right)$ | $\Delta\left(\ln C_{N T}\right)$ |
| :--- | :---: | :---: | :---: |
| $\Delta\left(\ln C_{N T t-5}\right)$ |  |  |  |
|  | -0.369737 | -0.102730 | 0.133995 |
|  | $(0.53274)$ | $(0.36233)$ | $(0.27680)$ |
| $\Delta\left(\ln C_{N T t-6}\right)$ | $[-0.69402]$ | $[-0.28353]$ | $[0.48408]$ |
|  |  |  |  |
|  | -0.314559 | -0.183349 | -0.319911 |
|  | $(0.45118)$ | $(0.30685)$ | $(0.23442)$ |
|  | $[-0.69720]$ | $[-0.59751]$ | $[-1.36469]$ |
| R-squared | 0.532972 | 0.548510 | 0.846678 |
| Sum sq. Resids. | 0.003921 | 0.001814 | 0.001059 |
| Log likelihood | 88.02603 | 99.20521 | 107.0135 |

Notes: Standard error in () and t-statistics in [ ].


[^0]:    ${ }^{1}$ For some parameter values, non-homothetic preferences can lead to unbalanced growth paths in which a sector of the economy disappears. The specification of preferences

    $$
    u=\left(\omega\left(C_{t}^{T}\right)^{-\eta}+(1-\omega)\left(\bar{c}+c_{t}^{N}\right)^{-\eta}\right)^{-\frac{1}{\eta}}
    $$

    allows for short-run non-homothetic behavior when $\bar{c} / c_{t}^{N}$ is large, and is consistent with balanced growth in the long run as $\bar{c} / c_{t}^{N} \rightarrow 0$. However, these preferences imply a demand function that is non-linear in the unknown parameter $\bar{c}$

    $$
    \ln \left(\frac{C_{t}^{N}}{C_{t}^{T}}\right)=\frac{1}{1+\eta} \ln \frac{1-\omega}{\omega}-\frac{1}{1+\eta} \ln p_{t}^{N}-\ln \left(1+\frac{\bar{c}}{c_{t}^{N}}\right)+\varepsilon_{t}
    $$

[^1]:    and is harder to estimate. Numerical simulations suggest that for over 100 years the model with the preference parameters estimated is well behaved.
    ${ }^{2}$ The authors constructed their own series following this methodology and obtained series for consumption of tradable and non-tradable goods that had a high correlation (between 0.60 and 0.98 ) with the series that were obtained from official sources. The latter were used because the levels of consumption seemed more plausible.

[^2]:    ${ }^{3}$ The Appendix presents the estimation of the complete model.

[^3]:    Notes: The number of lags in the test was selected using the Schwartz Information Criterion.

